

IOVS MS 09-4982 (Article 1229) Proofs Available

---

Dear Author:

The proofs of your article above are available for your review. Please download the file located at this URL address: <http://rapidproof.cadmus.com/RapidProof/retrieval/index.jsp>

Login: [your e-mail address]

Password: 77vZAHnLRRHQ

You will need to have Adobe Acrobat Reader software to read this file. This is free software and is available for user downloading at <http://www.adobe.com/products/acrobat/readstep.html>.

If you experience technical problems, please contact Tracey Ritchey (e-mail: [ritcheyt@cadmus.com](mailto:ritcheyt@cadmus.com); phone: 717-721-2646)

This file contains:

- Instructions to Author
- Adobe Acrobat Comments and Notes Instructions
- Publication Fees and Reprint Order Form
- Page Proofs for your article, table of contents precis blurb, and author queries - containing 7 pages

Please insert your comments electronically (instructions enclosed), or print the PDF proofs and add your comments manually. Follow the enclosed instructions for emailing, faxing, or mailing your corrections. Return all materials within 48 hours (two business days) to assure quick publication of your article.

NOTE: Effective with the January 2010 issue IOVS will be available online only. No printed issues will be produced. Printed reprints may still be ordered using the file provided.

If you have any questions regarding your article, please contact me. **ALWAYS INCLUDE YOUR ARTICLE NO. (IOVS MS 09-4982) WITH ALL CORRESPONDENCE.**

Cathy Frey

Tel: 717-721-2616

Fax: 717-738-9479 or 717-738-9478

[freyc@cadmus.com](mailto:freyc@cadmus.com)

# IOVS

## Investigative Ophthalmology & Visual Science

Dear Author:

Enclosed are page proofs for your manuscript to be published in *Investigative Ophthalmology & Visual Science*.

- Review these proofs carefully, as this is your final opportunity to correct the article prior to publication. (Your article has been copyedited to conform to journal style, and for grammar, punctuation, and consistency. You may find that changes have been made to clarify your meaning. If these changes do not alter the sense, let them stand. If your meaning has been altered, please suggest an alternative that will restore the correct meaning and clarify the passage.) See the enclosed instructions for editing proofs electronically.
- Proofread all tables and equations.
- Check that all non-English characters and symbols translated correctly.
- Please answer all author queries (AQ1, AQ2, etc.) listed on the last page of the article. Note that the Table of Contents précis blurb appears at the top of the Author Query page. The wording of the blurb may have been edited to comply with journal style.
- Check artwork carefully. All images in the PDF are reduced to low resolution and file size to facilitate internet delivery. These images will appear at higher resolution and sharpness in the published article. It will be assumed that COLOR reproductions are acceptable unless you contact Cadmus to express your dissatisfaction. You will NOT receive color prints for approval.
- Note: Once you have returned your proofs any changes will be treated as an Erratum; a fee of \$150 may apply.

**Within 48 hours (two business days), please return annotated or corrected page proofs by email, by fax, or by express mail/overnight service.**

**Email: [freyc@cadmus.com](mailto:freyc@cadmus.com)**

**FAX: 717-738-9479 or 717-738-9478**

**If you choose to send via express mail, address the package to my attention:**

Cathy Frey, Issue Management  
Cadmus Professional Communications  
Digital Publishing Services-Ephrata  
300 West Chestnut Street, Suite A  
Ephrata, PA 17522-1987, USA  
Tel: 717-721-2616

**PUBLICATION FEES AND REPRINT ORDERS:** Follow the instructions on the enclosed reprint order form. Send it under separate cover to the Philadelphia, Pennsylvania address listed on the reprint order form, or fax it to 877-705-1373.

Please note that the publication of your article may be delayed if you do not follow the above procedures. Contact me if you have any questions.

# Adding Comments and Notes to Your PDF

To facilitate electronic transmittal of corrections, we encourage authors to utilize the comments and notes features in Adobe Acrobat. The PDF provided has been "comment-enabled," which allows you to utilize the comments and notes features, even if using only the free Adobe Acrobat reader (see note below regarding acceptable versions). Adobe Acrobat's Help menu provides additional details about the tool. When you open your PDF, the comments/notes/edit tools are clearly shown on the tool bar. For purposes of correcting the PDF proof of your journal article, the important features to know are the following:

- Note tool (yellow text balloon icon): Click on this feature on the tool bar and then click on a point of the PDF where you would like to make a comment. This feature is useful when providing an instruction to your production contact or to verify a question or change that was posed.
- Text edits ("T" with strike-through and caret icon): The option Insert Text at Cursor allows the user to place the cursor at a point in text, which will then provide a pop-up box to add the appropriate text to be added to the proof.
- Highlight text ("T" with yellow highlight strike-through): The option Cross-Out Text Tool allows the user to indicate text that should be deleted from the proof. Click on this feature on the tool bar and highlight the text that is to be deleted.

As with hand-annotated proof corrections, the important points are to communicate changes clearly and thoroughly; to answer all queries and questions; and to provide complete information for us to make the necessary changes to your article so it is ready for publication.

To utilize the comments/notes features on this PDF you will need Adobe Reader version 7 or higher. This program is freely available and can be downloaded from <http://www.adobe.com/products/acrobat/readstep2.html>.

# Instructions for E-proofing

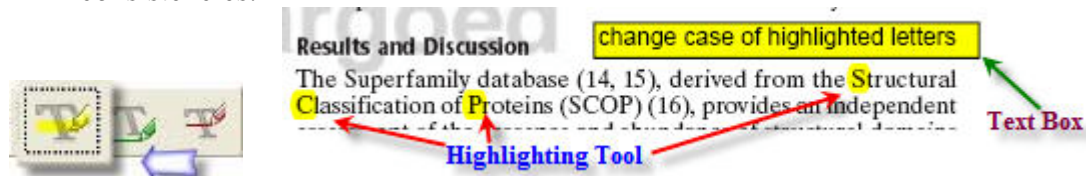
- Use Text Boxes and the Callout Tool to indicate changes to the text.



- Use the Strike-Out tool to indicate deletions to the text.



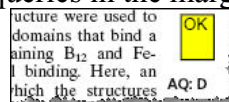
- Use the Highlighting Tool to indicate font problems, bad breaks, and other textual inconsistencies.



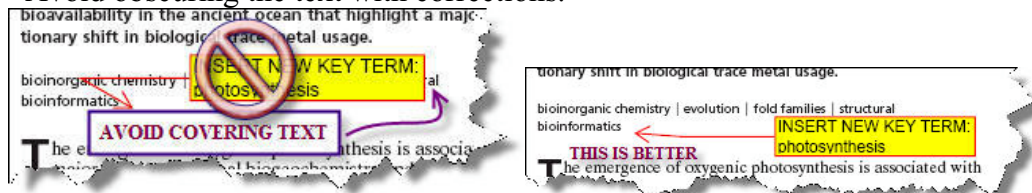
- Clearly indicate where changes need to be made using arrow, lines, and the Call-Out Tool.



- Mark changes and answer queries in the margins and other areas of white space.



- Avoid obscuring the text with corrections.



# Investigative Ophthalmology & Visual Science (IOVS) 2011

## This is your Publication Charges Notice and Reprint Order Form

**Pro Forma Invoice** (Please keep a copy of this document for your records.)

Reprint order forms and purchase orders or prepayments must be received 2 weeks before publication either by mail or by fax at 877-705-1373. It is the policy of Cadmus Reprints to not split invoices per order. **Please print clearly. Please return this form whether reprints are ordered or not as your Publication Charges will be invoiced to your attention.**

Author Name Li Wang  
Title of Article Total Corneal Power Estimation: Ray Tracing Method versus Gaussian Optics Formula  
Issue of Journal \_\_\_\_\_ Reprint # 3656616 Manuscript # 09-4982 Publication Date \_\_\_\_\_  
Number of Pages 7 Color in Article? Yes / No (Please Circle) Symbol IOVS

**Please include the journal name and reprint number or manuscript number on your purchase order or other correspondence.**

### Order and Shipping Information

#### Reprint Costs (Please see page 2 of 2 for reprint costs/fees.)

\_\_\_\_\_ Number of reprints ordered \$ \_\_\_\_\_  
\_\_\_\_\_ Number of color reprints ordered \$ \_\_\_\_\_  
\_\_\_\_\_ Number of B/W covers ordered \$ \_\_\_\_\_  
\_\_\_\_\_ Number of journal covers ordered \$ \_\_\_\_\_  
\_\_\_\_\_ Late order fee - file retrieval \$ \_\_\_\_\_

**Subtotal** \$ \_\_\_\_\_

Taxes \$ \_\_\_\_\_

*(Add appropriate sales tax for Virginia, Maryland, Pennsylvania, and the District of Columbia or Canadian GST to the reprints if your order is to be shipped to these locations.)*

First address included, add **\$32** for  
each additional shipping address \$ \_\_\_\_\_

#### Publication Fees (Please see page 2 of 2 for publication fees.)

Page charges: **\$70** per page for the 1<sup>st</sup> 8 pgs \$ \_\_\_\_\_  
Page charges: **\$150** for 9<sup>th</sup> & succeeding pgs \$ \_\_\_\_\_  
Color in journal: Add **\$100** per page with color \$ \_\_\_\_\_

**Total Amount Due** \$ \_\_\_\_\_

#### Shipping Address (cannot ship to a P.O. Box) Please Print Clearly

Name \_\_\_\_\_  
Institution \_\_\_\_\_  
Street \_\_\_\_\_  
City \_\_\_\_\_ State \_\_\_\_\_ Zip \_\_\_\_\_  
Country \_\_\_\_\_  
Quantity \_\_\_\_\_ Fax \_\_\_\_\_  
Phone: Day \_\_\_\_\_ Evening \_\_\_\_\_  
E-mail Address \_\_\_\_\_

#### Additional Shipping Address\* (cannot ship to a P.O. Box)

Name \_\_\_\_\_  
Institution \_\_\_\_\_  
Street \_\_\_\_\_  
City \_\_\_\_\_ State \_\_\_\_\_ Zip \_\_\_\_\_  
Country \_\_\_\_\_  
Quantity \_\_\_\_\_ Fax \_\_\_\_\_  
Phone: Day \_\_\_\_\_ Evening \_\_\_\_\_  
E-mail Address \_\_\_\_\_

\* Add \$32 for each additional shipping address.

### Payment and Credit Card Details

Enclosed: Personal Check \_\_\_\_\_  
Institutional Purchase Order \_\_\_\_\_  
Credit Card Payment Details \_\_\_\_\_

Checks must be paid in U.S. dollars and drawn on a U.S. Bank.

Credit Card:  VISA  Am. Exp.  MasterCard  
Card Number \_\_\_\_\_  
Expiration Date \_\_\_\_\_  
Signature: \_\_\_\_\_

Please send your order form and purchase order or prepayment made payable to:

**Cadmus Reprints**  
**P.O. Box 822942**  
**Philadelphia, PA 19182**

*Note: Do not send express packages to this location, PO Box.*  
FEIN #:540157890

### Invoice or Credit Card Information

#### Invoice Address Please Print Clearly

Please complete Invoice address as it appears on credit card statement

Name \_\_\_\_\_  
Institution \_\_\_\_\_  
Department \_\_\_\_\_  
Street \_\_\_\_\_  
City \_\_\_\_\_ State \_\_\_\_\_ Zip \_\_\_\_\_  
Country \_\_\_\_\_  
Phone \_\_\_\_\_ Fax \_\_\_\_\_  
E-mail Address \_\_\_\_\_  
Purchase Order No. \_\_\_\_\_

**Cadmus will process credit cards and Cadmus Journal Services will appear on the credit card statement.**

*If you do not mail your order form, you may fax it to 877-705-1373 with your credit card information.*

Signature \_\_\_\_\_ Date \_\_\_\_\_

Signature is required. By signing this form, the author agrees to accept the responsibility for the payment of reprints and/or all charges described in this document.

# Investigative Ophthalmology & Visual Science (IOVS) 2011

2011 Reprint Charges (No extra charge for color images). Author rates only. Not to be used for commercial ordering.

## Black and White and Color Reprint Prices

Domestic (USA only)					
# of Pages	100	200	300	400	500
1-4	\$420	\$535	\$650	\$760	\$870
5-8	\$775	\$935	\$1,085	\$1,225	\$1,400
9-12	\$1,100	\$1,340	\$1,540	\$1,775	\$2,040
13-16	\$1,480	\$1,750	\$2,000	\$2,245	\$2,550
17-20	\$1,695	\$2,050	\$2,415	\$2,700	\$3,100
21-24	\$1,950	\$2,300	\$2,700	\$3,000	\$3,450
25-28	\$2,280	\$2,625	\$3,135	\$3,450	\$3,995
29-32	\$2,600	\$3,000	\$3,530	\$3,995	\$4,500
B/W Cover	\$350	\$435	\$520	\$615	\$700
Journal Cover	\$1,350	\$1,435	\$1,520	\$1,620	\$1,715

International (includes Canada and Mexico)					
# of Pages	100	200	300	400	500
1-4	\$450	\$575	\$740	\$895	\$1,025
5-8	\$825	\$1,030	\$1,200	\$1,410	\$1,625
9-12	\$1,250	\$1,470	\$1,760	\$2,010	\$2,345
13-16	\$1,575	\$1,945	\$2,230	\$2,550	\$3,000
17-20	\$1,850	\$2,350	\$2,650	\$3,105	\$3,625
21-24	\$2,145	\$2,600	\$2,955	\$3,475	\$4,255
25-28	\$2,400	\$3,140	\$3,395	\$3,995	\$4,760
29-32	\$2,710	\$3,390	\$3,860	\$4,500	\$5,350
B/W Cover	\$355	\$440	\$525	\$620	\$705
Journal Cover	\$1,355	\$1,440	\$1,525	\$1,620	\$1,705

Minimum order is 100 copies. For orders larger than 500 copies, please consult Cadmus Reprints at 410-943-0629.

## B/W Cover

Cover prices are listed above. The cover will include the publication title, article title, and author name printed in black.

## Publication Fees

### Page Charges

Page charges: **\$70** per page for the first **8** pages; **\$150** per page for the **9<sup>th</sup>** and succeeding pages.

## Articles Published with Color Figures

If your article contains color illustrations, there will be a publishing charge to the author of **\$100** for each journal page that contains color. Please state exact color charge on the reverse side and add to your payment or purchase order accordingly.

## Shipping

Shipping costs are included in the reprint prices. Domestic orders are shipped via FedEx Ground service. Foreign orders are shipped via an expedited proof of delivery air service. The shipping address printed on an institutional purchase order always supercedes.

## Multiple Shipments

Orders can be shipped to more than one location. Please be aware that it will cost **\$35** for each additional location.

## Delivery

Your order will be shipped within 2 weeks of the journal online date. Allow extra time for delivery.

## Late Order Charges

Articles more than 90 days from publication date will carry an additional charge of \$50.00 per article for file retrieval.

## Tax Due

Residents of Virginia, Maryland, Pennsylvania, and the District of Columbia are required to add the appropriate sales tax to each reprint order. For orders shipped to Canada, please add 5% Canadian GST unless exemption is claimed.

## Ordering

Prepayment or a signed institutional purchase order is required to process your order. Please reference journal name and reprint number or manuscript number on your purchase order or other correspondence. You may use the reverse side of this form as a proforma invoice. Please return your publication charges form and reprint order form with purchase order or prepayment to:

### Cadmus Reprints

P.O. Box 822942  
Philadelphia, PA 19182-2942

**Note: Do not send express packages to this location, PO Box.**  
FEIN #:540157890

Please direct all inquiries to:

### June Billman

866-487-5625 (toll free number)  
410-943-3086 (direct number)  
877-705-1373 (FAX number)  
[june.billman@cenveo.com](mailto:june.billman@cenveo.com)

Reprint and Publication Charge Order Forms and Purchase Orders or prepayments must be received 2 weeks before publication.

Please return this form even if no reprints are ordered so publication fees may be invoiced.

# Total Corneal Power Estimation: Ray Tracing Method versus Gaussian Optics Formula

Li Wang,<sup>1</sup> Asbraf M. Mahmoud,<sup>2</sup> Betty Lise Anderson,<sup>3</sup> Douglas D. Koch,<sup>1</sup> and Cynthia J. Roberts<sup>2</sup>

**PURPOSE.** To evaluate with the use of corneal topographic data the differences between total corneal power calculated using ray tracing (TCP) and the Gaussian formula (GEP) in normal eyes, eyes that previously underwent laser in situ keratomileusis/photorefractive keratectomy (LASIK/PRK), and theoretical models.

**METHODS.** TCP and GEP were calculated over the central 4-mm zone using mean instantaneous curvature in 94 normal eyes, 61 myopic-LASIK/PRK eyes, and 9 hyperopic-LASIK/PRK eyes. A corneal model was constructed to assess the incident angles at the posterior corneal surface for both refracted rays and parallel rays. Corneal models with varying parameters were also constructed to investigate the differences between mean TCP and GEP (4-mm zone), and an optical design software validation was performed.

**RESULTS.** The TCP values tended to be less than GEP in normal and myopic-LASIK/PRK eyes, with the opposite relationship in some hyperopic-LASIK/PRK eyes having the highest anterior surface curvature. The difference between TCP and GEP was a function of anterior surface instantaneous radii of curvature and posterior/anterior ratio in postrefractive surgery eyes but not in normal eyes. In model corneas, posterior incident angles with parallel rays were greater than those with refracted rays, producing an overestimation of negative effective posterior corneal power; differences in magnitude between TCP and GEP increased with decreasing ratio of posterior/anterior radii of curvature, consistent with clinical results.

**CONCLUSIONS.** In eyes after refractive surgery, calculating posterior corneal power using the Gaussian formula and its paraxial assumptions introduces errors in the calculation of total corneal power. This may generate errors in intraocular lens power calculation when using the Gaussian formula after refractive surgery. (*Invest Ophthalmol Vis Sci.* 2011;52:000-000) DOI: 10.1167/iovs.09-4982

Accurate estimation of the total corneal refractive power is important in the calculation of intraocular lens power. Traditionally, anterior corneal curvature is measured using a

keratometry or computerized videokeratography (CVK). To compensate for posterior corneal curvature, keratometers and CVK devices use a standardized index of refraction to convert measurements of anterior corneal curvature to the refractive power of the entire cornea. In most keratometers and CVK devices, a value of 1.3375 is used that is based on the assumption of a single refracting surface. Clinically, this methodology has provided acceptable values for tasks such as intraocular lens calculations in normal, unoperated corneas. However, in eyes that have previously undergone ablative corneal refractive surgery (e.g., excimer laser photorefractive keratectomy [PRK] or laser in situ keratomileusis [LASIK]), the relationship between the front and the back surfaces of the cornea has been altered,<sup>1,2</sup> and the use of the standardized index of refraction of 1.3375, which does not account for the altered relationship between the anterior and posterior surfaces, is no longer valid.<sup>3</sup>

Because of the development of scanning slit and Scheimpflug technology for topographic devices, it is now possible to measure posterior corneal curvature. Total corneal power can be calculated based on measurements of anterior and posterior corneal curvatures and corneal thickness. Methods for calculating total corneal power include ray tracing and the Gaussian optics thick lens formula.<sup>4-6</sup>

The purposes of the present study were to evaluate in normal corneas and corneas that had undergone LASIK/PRK the differences between values for total corneal power calculated using the ray tracing method (with Snell's Law refraction at both the anterior and the posterior surfaces) and the Gaussian optics formula and to further explore in theoretical model eyes the factors contributing to these differences.

## PATIENTS AND METHODS

### Analysis in Clinical Subjects

We obtained institutional review board approval for this study. This research adhered to the tenets of the Declaration of Helsinki. Retrospectively, we reviewed consecutive cases of subjects who visited Baylor College of Medicine during January 2008 to October 2008. Inclusion criteria were patients who underwent no previous corneal or ocular surgery in the normal group or who underwent LASIK at least 3 months previously or PRK at least 6 months previously and patients who had Galilei (Galilei Dual Scheimpflug Analyzer; Ziemer Ophthalmics AG, Port, Switzerland) measurements with good quality (quality okay check mark displayed on the Galilei maps).

Three groups were included: (1) 94 eyes of 58 patients in the normal eye group; the mean ( $\pm$ SD) age was  $36 \pm 11$  years (range, 20-62 years); these subjects were selected from the patients screened for corneal refractive surgery; (2) 61 eyes of 36 patients in the myopic-LASIK/PRK group; the mean age was  $38 \pm 9$  years (range, 21-54 years), and the myopic correction was  $-3.66 \pm 1.66$  D (range, -7.58 to -1.00 D); (3) 9 eyes of 5 patients in the hyperopic-LASIK/PRK

From the <sup>1</sup>Department of Ophthalmology, Baylor College of Medicine, Houston, Texas; and the Departments of <sup>2</sup>Ophthalmology and Biomedical Engineering and <sup>3</sup>Electrical and Computer Engineering, The Ohio State University, Columbus, Ohio.

Supported by an unrestricted grant from Research to Prevent Blindness and by The Ohio Lions Eye Research Foundation.

Submitted for publication November 25, 2009; revised July 23 and August 10, 2010; accepted October 10, 2010.

Disclosure: **L. Wang**, Ziemer Ophthalmics AG (F); **A.M. Mahmoud**, Ziemer Ophthalmics AG (F); **B.L. Anderson**, None; **D.D. Koch**, None; **C.J. Roberts**, Ziemer Ophthalmics AG (F, C)

Corresponding author: Li Wang, Department of Ophthalmology, Baylor College of Medicine, 6565 Fannin Street, NC-205, Houston, TX 77030; liw@bcm.tmc.edu.



group; the mean age was  $52 \pm 4$  years (range, 45–54 years), and the hyperopic correction was  $+2.30 \pm 1.10$  D (range, +1.00 to +4.46 D).

### Ray Tracing Method

The analyzer we used (Galilei Dual Scheimpflug Analyzer; Ziemer Ophthalmics AG) combines dual-channel Scheimpflug cameras with an integrated Placido disc to measure both anterior and posterior corneal surfaces and corneal thickness. The Galilei calculates the total corneal power (TCP) using ray tracing, which propagates incoming parallel rays and uses Snell's law to refract these rays through the anterior and posterior corneal surfaces. Power is determined by  $n/f$ , based on the calculated focal length ( $f$ ), which is referenced to the anterior corneal surface, and  $n$  is the index of refraction of the aqueous ( $n = 1.336$ ). TCP values over the central, paracentral, and peripheral zones are displayed. We recorded the average TCP over the central 4-mm area for each eye and used the index of refraction of the aqueous ( $n = 1.336$ ) to convert ray traced focal length to power.

### Gaussian Formula

The Gaussian formula calculates Gaussian equivalent power (GEP) by assuming paraxial imaging and combining two lenses separated by the central corneal thickness:

$$GEP = F1 + F2 - (d/n)(F1 * F2)$$

where  $F1$  = anterior corneal power,  $F2$  = posterior corneal power,  $d$  = pachymetry, and  $n$  = index of refraction (1.376). In this study, the  $F1$  value was calculated using a paraxial formula<sup>5</sup> by converting the average central instantaneous curvature (central 4-mm zone) displayed on the Galilei in diopters to anterior power by multiplying by 376/337.5. The  $F2$  value was the posterior average central instantaneous curvature, for which the dioptric value displayed on the Galilei was calculated using the same paraxial formula with both the corneal (1.376) and the aqueous (1.336) indices of refraction. The pachymetric value used was the average over the central 4-mm area, as displayed on the Galilei. As with most corneal topographers, the posterior curvature is converted to diopters using the same formula as the anterior surface, assuming that incoming rays are parallel. It should also be noted that the GEP is referenced to the second principal plane, which is distinct from the TCP calculation, which is referenced to the anterior corneal surface.

### Data Analysis

The differences between the TCP and GEP were calculated in the three groups of patients. Student's  $t$ -test was used to compare the TCP and GEP, and correlation analysis was performed to assess the relationship between the differences of TCP and GEP and the anterior instantaneous radii of curvature as well as the posterior/anterior ratio. Statistical analysis was performed using statistical analysis software (SPSS, version 15.0; SPSS, Inc., Chicago, IL), and  $P \leq 0.05$  was considered statistically significant.

### Theoretical Analysis

**Model with Average Parameters in Normal Eyes.** A corneal model was constructed using the mean values found in the normal eyes included in this study (anterior radius of curvature,  $r1 =$

7.7 mm; posterior radius of curvature,  $r2 = 6.3$  mm; and central pachymetry = 0.56 mm). The incident angles at the posterior corneal surfaces were calculated in the ray tracing method by refracting incoming parallel rays at the anterior corneal surface using Snell's law. The differences in incident angles between these refracted and parallel rays were analyzed. Furthermore, values for effective posterior corneal power (EPP) were calculated using the ray traced angle of incidence on the posterior surface and the refracted angle through the posterior surface. Therefore, EPP is the ray traced power of the posterior surface using nonparallel rays refracted by the anterior surface that have been propagated through the corneal thickness. This power is referenced to the posterior surface with  $n1 = 1.376$  and  $n2 = 1.336$ . EPP values were then compared to values for posterior corneal powers used in the Gaussian formula (GPP), which were determined by the topographer using the paraxial approximation ( $GPP = (1336 - 1376)/r2$ , where  $r2 =$  posterior corneal radius of curvature), which is based on the assumption of parallel rays approaching the posterior corneal surface.

**Model with Varying Parameters.** A set of theoretical corneas with two spherical surfaces representing the anterior and posterior corneal surfaces was constructed. The anterior corneal radius of curvature ranged from 6.5 mm to 10.0 mm, in 0.25-mm steps. The ratio of posterior to anterior radii of curvature ranged from 0.7 to 0.9, in 0.025 steps. Central pachymetry ranged from 450  $\mu$ m to 550  $\mu$ m, in 25- $\mu$ m steps. Rays of light were propagated through both surfaces assuming indices of refraction as follows: air = 1.0, cornea = 1.376, and aqueous = 1.336. Average TCP and GEP within the central 4-mm zone were calculated for each posterior/anterior ratio and pachymetry. These average values were calculated using the same zone as that used in the clinical patients. The differences between TCP and GEP (TCP – GEP) were analyzed as functions of ratio of posterior/anterior radius of curvature, pachymetry, and anterior corneal power.

The same sets of theoretical corneas were implemented in optical design software (ZEMAX; ZEMAX Development Corp., Bellevue, WA). The surfaces were spherical. The pupil (aperture stop) measured 2 mm in radius. The value for pachymetry was assumed in ZEMAX to be apex to apex (e.g., measured along the axis); the thickness was therefore not uniform. The input was a set of rays traveling parallel to the optical axis and filling the pupil. The focal point was calculated to be where the radial spot size was minimized, using nonparaxial ray calculations. The effective focal length (EFL) referred to air is reported by ZEMAX, referenced to the second principal plane. The power computed from the EFL is Power =  $1/EFL$ (meters).

## RESULTS

### Clinical Subjects

Anterior and posterior instantaneous radii of curvature values are shown in Table 1. The mean ratio of posterior/anterior instantaneous radii of curvature was 0.82 in normal eyes, 0.76 in myopic-LASIK/PRK eyes, and 0.86 in hyperopic-LASIK/PRK eyes. Values for TCP calculated using ray tracing and for GEP calculated with the Gaussian formula are shown in Table 2. TCP tended to be less than GEP in normal and myopic-LASIK/PRK eyes, with the opposite relationship in some hyperopic-LASIK/PRK eyes having the highest anterior surface curvature. In general, the absolute differences between the TCP and GEP

TABLE 1. Anterior, Posterior, and Ratio of Posterior/Anterior Instantaneous Radii of Curvature

	Anterior (mm)	Posterior (mm)	Ratio (posterior/anterior)
Normal eyes ( $n = 94$ )	$7.69 \pm 0.24$ (7.25–8.28)	$6.27 \pm 0.25$ (5.71–7.04)	$0.82 \pm 0.02$ (0.73–0.87)
Myopic-LASIK/PRK eyes ( $n = 61$ )	$8.29 \pm 0.34$ (7.46–9.08)	$6.34 \pm 0.26$ (5.60–6.81)	$0.76 \pm 0.03$ (0.69–0.83)
Hyperopic-LASIK/PRK eyes ( $n = 9$ )	$7.46 \pm 0.14$ (7.30–7.68)	$6.40 \pm 0.17$ (6.20–6.63)	$0.86 \pm 0.02$ (0.82–0.91)

Values are mean  $\pm$  SD (range).

AQ: 3

AQ: 4

AQ: 5

T1

T2



TABLE 2. TCP Using the Ray Tracing Method and the GEP Calculated with the Gaussian Formula

	TCP (D)	GEP (D)	Difference (D)
Normal eyes ( <i>n</i> = 94)	42.27 ± 1.33 (39.26–44.96)	42.71 ± 1.33 (39.65–45.29)	−0.44 ± 0.20 (−0.89 to 0.72)
Myopic-LASIK/PRK eyes ( <i>n</i> = 61)	38.65 ± 1.82 (34.48–42.86)	39.20 ± 1.72 (35.47–43.40)	−0.55 ± 0.29 (−1.37 to 0.08)
Hyperopic-LASIK/PRK eyes ( <i>n</i> = 9)	44.41 ± 1.11 (42.82–45.64)	44.33 ± 0.87 (43.02–45.64)	0.08 ± 0.47 (−0.84 to 0.71)

Values are mean ± SD (range).

tended to increase with increasing anterior instantaneous radii of curvature in hyperopic-LASIK/PRK eyes with TCP > GEP and to decrease in myopic LASIK/PRK eyes with TCP < GEP, whereas normal eyes showed no relationship with anterior surface curvature (Fig. 1). The Pearson correlation coefficient values were 0.064 (*P* = 0.543) in normal eyes, −0.232 (*P* = 0.069) in myopic-LASIK/PRK eyes, and −0.313 (*P* = 0.412) in hyperopic-LASIK/PRK eyes. If the postrefractive surgery eyes were grouped together, the Pearson correlation coefficient value was −0.504 (*P* < 0.001). Note that without the single outlier in the normal population, the range of difference is <1 D in normal eyes and approximately 1.5 D in eyes after refractive surgery. The differences between TCP and GEP were also a function of posterior/anterior ratio in eyes after refractive surgery, whereas no relationship was found in normal eyes (Fig. 2). Differences were greatest at the lowest ratios in myopic LASIK/PRK eyes.

**Theoretical Analysis**

**Model with Average Parameters in Normal Eyes.** With r1 of 7.7 mm, r2 of 6.3 mm, and pachymetry of 0.56 mm at the posterior corneal surface, the incident angles with parallel rays were greater than the incident angles with rays refracted by the anterior corneal surface. The difference in incident angles between the parallel rays and the refracted rays increased with increasing distance from the center. The differences between EPP and GPP decreased with increasing anterior corneal radius of curvature (decreasing curvature) and increased with increasing distance from the center of the cornea (Fig. 3).

**Model with Varying Parameters.** As the ratio of posterior/anterior radius of curvature decreased, the magnitude of the absolute differences between TCP and GEP increased. The

average differences for anterior corneal radii of curvature from 6.5 mm to 10.0 mm (anterior corneal powers from 57.9 D to 37.6 D) ranged from −0.54 D for a ratio of 0.7 to −0.45 D for a ratio of 0.9 (Fig. 4). As central corneal thickness increased, the differences between TCP values and GEP values decreased; assuming a constant ratio for posterior/anterior radius of curvature of 0.8 and an anterior radius of curvature of 7.5 mm, the differences ranged from −0.46 D for thickness of 0.45 mm to −0.63 D for thickness of 0.55 mm (Fig. 5). As anterior corneal radius of curvature increased, the differences between TCP and GEP decreased (Fig. 6).

The result of the ZEMAX validation is shown in Figure 7 and indicates that in theoretical surfaces, both GEP and TCP show excellent correlation with the ZEMAX reference. The differences between the intercepts of the two formulas lie in their distinct references, with GEP and ZEMAX referenced to the second principal plane, whereas TCP is referenced to the anterior corneal surface.

**DISCUSSION**

Accurate estimation of corneal refractive power is critical in the calculation of intraocular lens power. Because it is possible to obtain measurements of posterior corneal curvature, total corneal power can be determined using either the Gaussian optics thick lens formula or ray tracing. Traditionally, the Gaussian formula has been used to calculate the equivalent corneal power.<sup>7,8</sup> However, the dual Scheimpflug topographer used in this study also calculates total corneal power using the ray tracing method. To the best of our knowledge, this is the first study to compare the differences between values for total

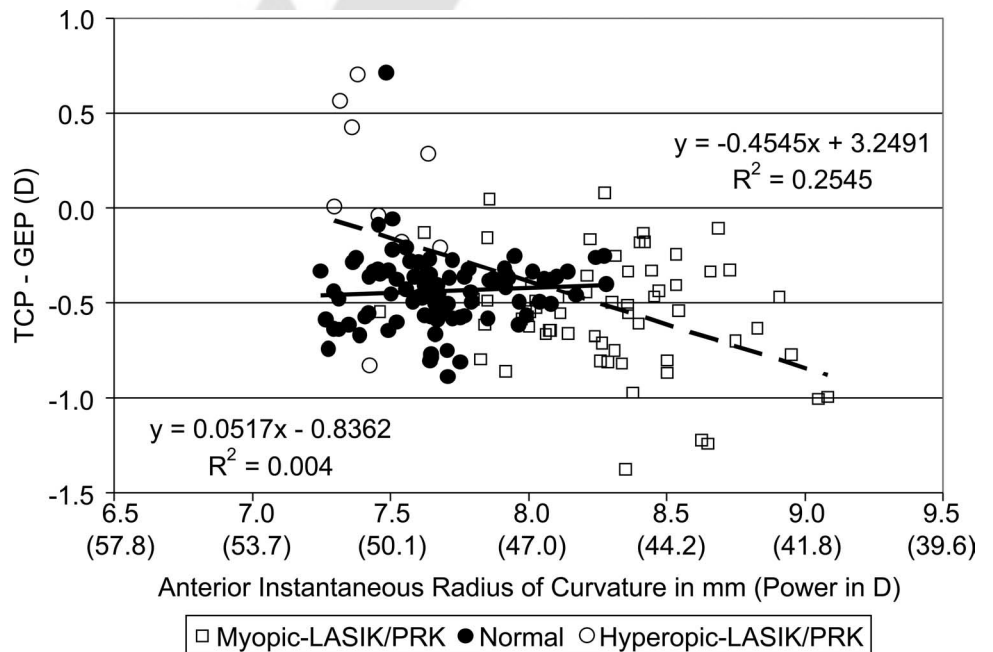
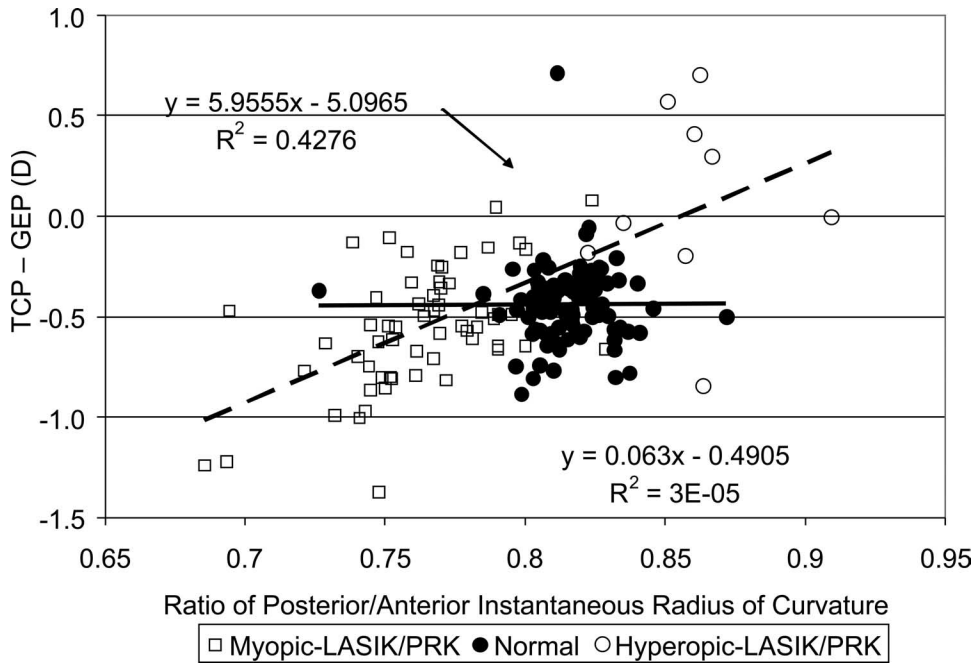


FIGURE 1. Differences between the TCP with the ray tracing from the Galilei and GEP using the Gaussian formula as a function of the anterior instantaneous radii of curvature. In post-refractive surgery eyes, the differences in magnitude between the TCP and GEP increased with increasing anterior instantaneous radii of curvature. The Pearson correlation coefficient value was −0.504 (*P* < 0.001).



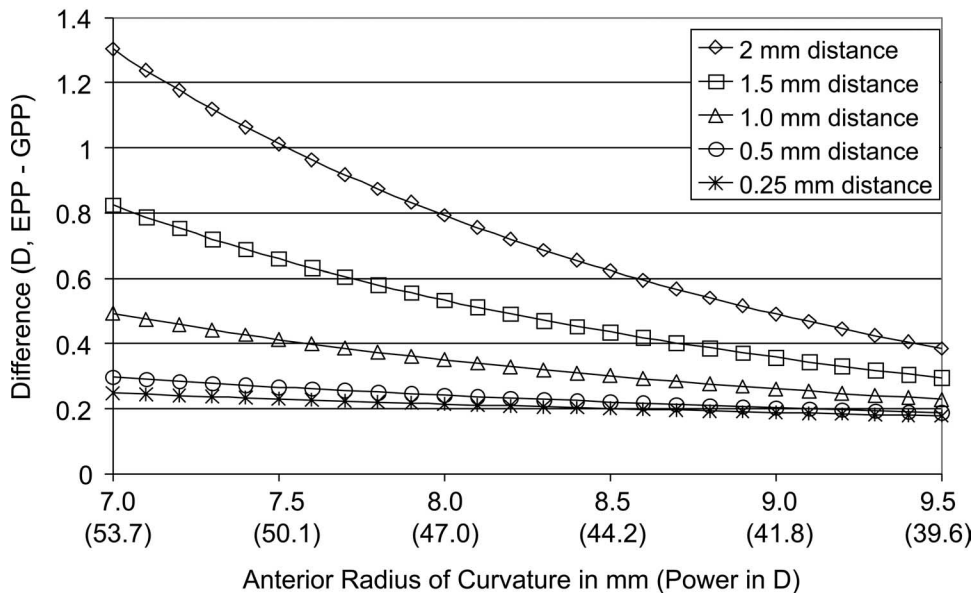
**FIGURE 2.** Differences between the TCP with the ray tracing from the Galilei and GEP using the Gaussian formula as a function of ratio of posterior/anterior instantaneous radius of curvature. In post-refractive surgery eyes, the differences in magnitude between the TCP and GEP increased with decreasing ratio. The Pearson correlation coefficient value was 0.654 ( $P < 0.001$ ).

corneal power calculated using ray tracing and the Gaussian formula.

Our results showed that ray tracing calculated lower values for corneal power than did the Gaussian formula for postmyopic LASIK eyes and normal eyes (mean differences of  $-0.55$  D and  $-0.44$  D, respectively) and a slightly higher mean difference of  $+0.08$  D for posthyperopic LASIK eyes. One source for the differences between TCP and GEP is the distinct reference, with TCP referenced to the anterior surface of the cornea and GEP to the second principal plane, in front of the cornea. In normal eyes, the differences between TCP and GEP are independent of anterior surface curvature and posterior-anterior ratio. However, after refractive surgery, the differences between TCP and GEP are a function of both posterior/anterior ratio and anterior surface curvature. This is likely due to the

dramatically altered surface profile after refractive surgery, which changes the region over which paraxial calculations are appropriate. Consistent with theoretical predictions, the lower anterior/posterior radius of curvature ratio in the myopic group was associated with the greatest absolute differences between TCP and GEP, resulting from error in the use of paraxial topography-driven values for F2 in the GEP formula. Interestingly, theoretical surfaces predicted that greater anterior surface curvature would result in the greatest absolute difference between TCP and GEP. However, this was not consistent with clinical results, which showed that the greatest absolute differences were at the lowest anterior surface curvature in the myopic group. This leads to the conclusion that the posterior/anterior ratio has a stronger impact on the magnitude of the difference in TCP and GEP than anterior surface curva-

**Posterior Power Error vs. Anterior Radius of Curvature**  
( $r_2=6.3\text{mm}$ , pachymetry= $0.56\text{mm}$ )



**FIGURE 3.** Differences between EPP determined by the ray tracing method from the Galilei and the posterior corneal power calculated using the GPP as functions of anterior corneal radii of curvature and the distance from the center of the cornea ( $r_2$  = posterior corneal radius of curvature).

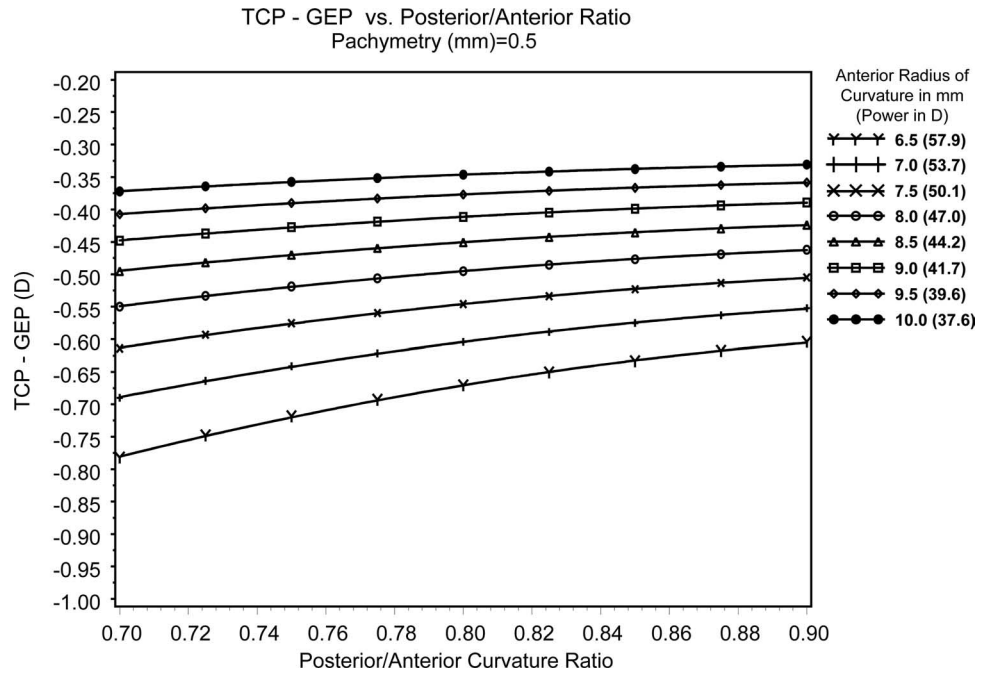


FIGURE 4. Differences between the TCP using the ray tracing method from the Galilei and GEP with the Gaussian formula as a function of ratio of posterior/anterior radius of curvature with a constant central pachymetry of 0.5 mm.

ture and that the paraxial region of both the anterior and the posterior surfaces interact to determine the size of the valid paraxial region, especially after refractive surgery.

Figures 1 and 2 provide insight into the source of error in calculating intraocular lens (IOL) power after refractive surgery. Although the average differences between TCP and GEP were similar in myopic subjects and normal subjects, the variability was much higher in the postrefractive surgery subjects. Without the single outlier in the normal group, the variability would have been approximately half that of either the myopic or the hyperopic subjects. In addition, there was a significant relationship between the TCP-GEP difference and both the posterior/anterior ratio and anterior surface curvature in eyes after refractive surgery. These relationships are absent in nor-

mal eyes. The distribution of the error function in the normal population confirms what clinical experience has shown: there would be acceptable accuracy with IOL calculations that use an empiric formula with an assumed posterior surface. However, the distribution of the error function of both the hyperopic and the myopic subjects unfortunately also confirms clinical experience that, because of the variability in these populations and the significant slope with changing anterior curvature and posterior/anterior ratio, standard IOL calculation formulas are not sufficiently accurate for these eyes. Therefore, we believe that, in eyes that have undergone LASIK/PRK, the use of values for total corneal power calculated with ray tracing will prove to be superior to corneal power calculations based on the anterior curvature alone or the GEP.

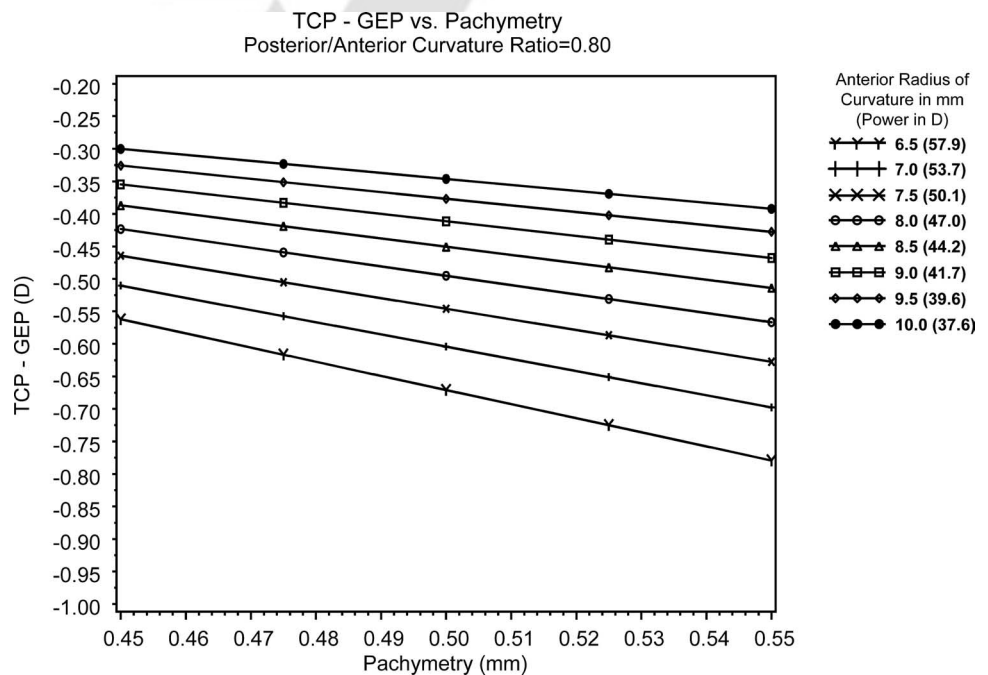


FIGURE 5. Differences between the TCP using the ray tracing method from the Galilei and GEP with the Gaussian formula as a function of pachymetry with a constant ratio of posterior/anterior radius of curvature of 0.8.

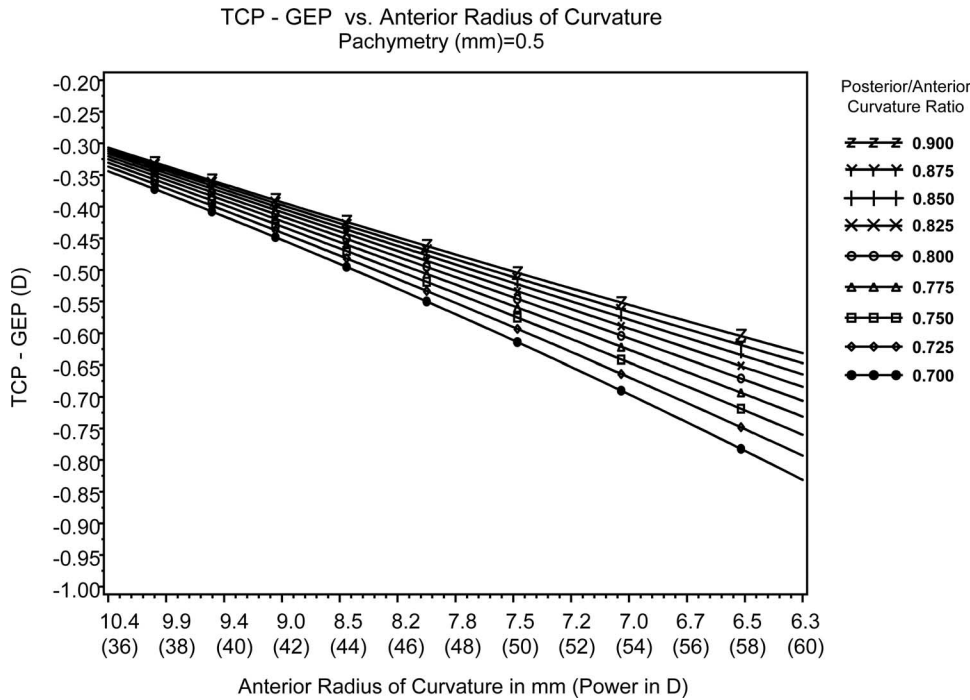


FIGURE 6. Differences between the TCP using the ray tracing method from the Galilei and GEP with the Gaussian formula as a function of anterior corneal radius of curvature.

In studies using an automatically rotating Scheimpflug camera (Pentacam; Oculus, Wetzlar, Germany) to measure normal corneas, the equivalent corneal power calculated using the Gaussian formula was consistently lower than the simulated keratometry (SimK) obtained from various devices by 1.2 to 1.3 D (Table 3).<sup>6,7</sup> Using optical coherence tomography (OCT), in normal eyes, the total corneal power calculated by the summation of the anterior and posterior corneal powers underestimated the Atlas SimK (Humphrey Atlas; Carl Zeiss Meditec, Jena, Germany) by 1.13 D.<sup>9</sup> The contribution of corneal thickness in the Gaussian formula is around 0.1 D, indicating that the Gaussian formula using the OCT would have underestimated the SimK by approximately 1.23 D. These reported

differences between the SimK and the equivalent corneal power calculated with the Gaussian formula are consistent with our finding of 1.30 D using the Galilei (Table 3).

The SimK is an estimation of total corneal power based on anterior corneal curvature and keratometric index of refraction, by modeling the cornea as a single refracting surface. Norrby<sup>10</sup> pointed out that the commonly used index of refraction of 1.3375 gives the power at the posterior vertex of the cornea, and an index of 1.3315 proposed by Olsen<sup>11</sup> gives the power at the second principal plane, which is approximately 0.8 D less than at the posterior vertex. Estimated corneal power is further reduced by about another 0.5 D<sup>9</sup> when the recently reported lower posterior/anterior ratio of 0.813 is

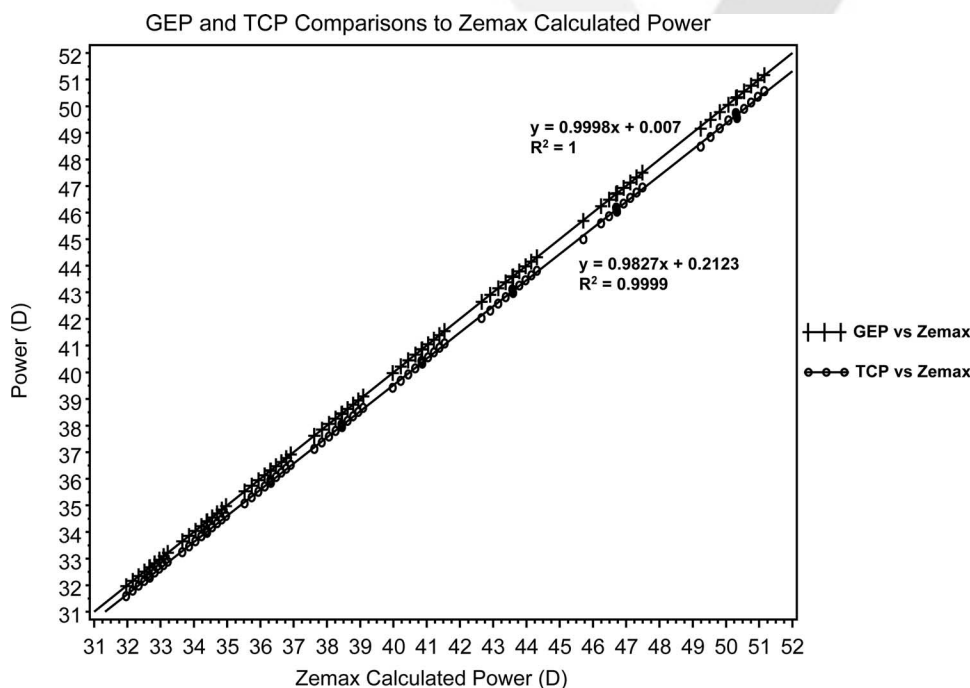


FIGURE 7. Plots of the TCP using the ray tracing method from the Galilei versus ZEMAX calculated power and GEP versus ZEMAX calculated power for theoretical corneas with excellent correlations (both Pearson correlation coefficient values  $R > 0.99$ ;  $P < 0.001$ ).



TABLE 3. Summary of Studies Comparing the SimK and Equivalent Corneal Powers Calculated with the GEP

Study	Corneas	Device for SimK	Device for GEP	Difference SimK-GEP (D)
Borasio et al <sup>6</sup>	Normal	Topcon (Oakland, NJ)	Pentacam	1.30
Savini et al <sup>7</sup>	Normal	TMS-2 (Tomey, Phoenix, AZ)	Pentacam	1.20
		Keratron (Optikon, Rome, Italy)	Pentacam	1.29
		Pentacam	Pentacam	1.25
Tang et al <sup>8</sup>	Normal	Humphrey Atlas	OCT*	1.13
Current study	Normal	Galilei	Galilei	1.30

\* OCT calculates TCP by summing anterior and posterior corneal powers, not including the contribution of corneal thickness.

used<sup>12</sup> instead of the Gullstrand ratio of 0.883 (6.8/7.7). However, because of variation in the population in the ratio of posterior to anterior corneal radius of curvature, especially in eyes after corneal refractive surgery, a single index of refraction is not sufficient, and the accuracy of SimK in estimating the total corneal power is poor.

This study had several limitations: a small number of eyes were included in the hyperopic-LASIK/PRK group; spherical surfaces were used in the theoretical models; in normal corneas, especially corneas after myopic or hyperopic LASIK/PRK, corneal surfaces are not spherical; the relative accuracy of using ray tracing for the prediction of IOL power must be validated in the clinical setting; and the TCP calculated using the ray tracing method is the power at the anterior vertex of the cornea, and the GEP using the Gaussian formula is the power at the second principal plane. The second principal plane of the cornea is approximately 0.05 mm in front of the anterior corneal vertex,<sup>15</sup> which produces a power difference of <0.1 D. This magnitude of difference is small in comparison with the mean differences of  $\geq 0.4$  D between TCP and GEP found in healthy clinical subjects and those after myopic refractive surgery. It is important to note that, to the best of our knowledge, posterior corneal power is not accurately represented in any corneal topographer or anterior segment imaging device because radius of curvature is converted to diopters using a paraxial formula that does not account for a Snell's law refraction, as has been described for the anterior surface.<sup>6</sup> In addition, the rays propagating to the posterior surface have already been refracted by the anterior surface; therefore, the "effective" posterior power will be less than what is calculated using parallel incident rays and a paraxial formula.

In conclusion, this study demonstrated that the Gaussian formula overestimated total corneal power in most clinical subjects and in theoretical models. The paraxial assumption inherent in the Gaussian formula generates variable errors in eyes after refractive surgery. The errors vary according to anterior corneal curvature, ratio of posterior/anterior radii of curvature, distance from the center of the cornea, and corneal thickness. Ray tracing does not rely on paraxial optics and is

the better method with which to calculate total corneal refractive power.

## References

- Hugger P, Kohnen T, La Rosa FA, Holladay JT, Koch DD. Comparison of changes in manifest refraction and corneal power after photorefractive keratectomy. *Am J Ophthalmol*. 2000;129:68-75.
- Hamed AM, Wang L, Misra M, Koch DD. A comparative analysis of five methods of determining corneal refractive power in eyes that have undergone myopic laser in situ keratomileusis. *Ophthalmology*. 2002;109:651-658.
- Seitz B, Langenbucher A. Intraocular lens calculations status after corneal refractive surgery. *Curr Opin Ophthalmol*. 2000;11:35-46.
- Freeman MH. *Optics*. 10th ed. London: Butterworths; 1990:115-120.
- Harris WF. Effective corneal refractive zone in terms of Gaussian optics. *J Cataract Refract Surg*. 2008;34:2030-2035.
- Roberts C. The accuracy of power maps to display curvature data in corneal topography systems. *Invest Ophthalmol Vis Sci*. 1994;35:3525-3532.
- Borasio E, Stevens J, Smith GT. Estimation of true corneal power after keratorefractive surgery in eyes requiring cataract surgery: BESS formula. *J Cataract Refract Surg*. 2006;32:2004-2014.
- Savini G, Barboni P, Carbonelli M, Hoffer KJ. Agreement between Pentacam and videokeratography in corneal power assessment. *J Refract Surg*. 2009;25:534-538.
- Tang M, Li Y, Avila M, Huang D. Measuring total corneal power before and after laser in situ keratomileusis with high-speed optical coherence tomography. *J Cataract Refract Surg*. 2006;32:1843-1850.
- Norrby S. Pentacam keratometry and IOL power calculation. *J Cataract Refract Surg*. 2008;34:3.
- Olsen T. On the calculation of power from curvature of the cornea. *Br J Ophthalmol*. 1986;70:152-154.
- Dubbelman M, Van der Heijde GL, Weeber HA, Vrensen GF. Radius and asphericity of the posterior corneal surface determined by corrected Scheimpflug photography. *Acta Ophthalmol Scand*. 2002;80:379-383.
- Norrby NE. Unfortunate discrepancies. *J Cataract Refract Surg*. 1998;24:433-434.

## TABLE OF CONTENTS PRECIS BLURB

The paraxial assumption inherent in the Gaussian formula generates variable errors in eyes after refractive surgery. The errors vary according to anterior corneal curvature, ratio of posterior/anterior radii of curvature, distance from the center of the cornea, and corneal thickness.

## AUTHOR QUERIES

### AUTHOR PLEASE ANSWER ALL QUERIES

1

AQ1: Has IOL been written out correctly here and in the text?

AQ2: Please confirm whether the interchangeable use of 'patients' and 'subjects' is correct or change as necessary for consistency.

AQ3: To conform to journal style, your article has been edited to place commercial or trade names inside parentheses following their generic equivalent or description. (With the exception of ZEMAX and Galilei, because these products are integral to your study, commercial or trade names may not be mentioned in the text flow.) Please keep this restriction in mind if you wish to revise the edited wording.

AQ4: Please include the units for the ratio of posterior to anterior radii of curvature.

AQ5: All tables and display math are manually typeset by the compositor. Please check carefully. In Table 3, please verify the manufacturer/location for TMS-2 as inserted by the copy editor.

